# Year 4 Learning and Progression Steps for Mathematics

## What are Learning and Progression Steps (LAPS)?

The Learning and Progression Steps are designed to scaffold the learning required in order to meet the expectations of the National Curriculum. Statements in the Lancashire Key Learning for Mathematics document have been broken down into smaller steps to support teachers in planning appropriate learning opportunities. These key pieces of learning will support pupils in becoming fluent in the knowledge and skills of the curriculum and ensure that the learning is effective and sustained.

The number of steps is dependent on the learning and do **not** constitute expectations for the end of each term.

Orange (including the end of previous year expectation) are the steps in learning for the autumn term.

Green are the steps in learning for the spring term.

Yellow are the steps in learning for the summer term and incorporate the end of year expectations.

The colours correspond with the structure of the Lancashire Mathematics Curriculum and reflect how often each learning objective is explicitly taught across the year. Some key learning objectives are not taught in every term, and in some cases not in the summer term. This means that end of year expectations may need to be met before the end of the summer term.

The final step in the progression for each strand of learning is the end of year expectation.

The steps are not of equal size and different amounts of time may be required for children to move between individual steps. For example,



Some learning within the same end of year expectation has been split and designed to run concurrently alongside each other. For example,

Read and write numbers	numerals and in words	numerals and in words	Read numbers to 10 000 where 0 is not used as a place holder	Read numbers to 10 000 where 0 is used as a place holder	Read and write numbers to at least
up to 1000 in numerals	Write multiples of 1000 to 10 000 in	Write multiples of 100 to 10 000 in	Write numbers to 10 000 where 0 is	Write numbers to 10 000 where 0 is	10 000
and in words	numerals and in words	numerals and in words	not used as a place holder	used as a place holder	

Some LAPS may need to be completed before another can be started.

#### Where have they come from?

The Learning and Progression Steps (LAPS) have been derived from the Lancashire Key Learning in Mathematics statements, identified primarily from the National Curriculum 2014 programmes of study.

#### How are they different from the Key Learning Statements?

The Learning and Progression Steps (LAPS) are smaller, progressive steps which support learning towards the Key Learning in Mathematics expectations.

#### How are they different from the Key Learning Indicators of Performance (KLIPs)?

The Key Learning Indicators of Performance (KLIPs) document is an assessment tool. The Learning and Progression Steps (LAPS) document is a planning tool and is not intended to be used for summative assessment purposes. However, they may support teachers in judging whether children are on track to meet the end of year expectations at different points throughout the year.

The terms 'entering', 'developing' and 'secure' are used in Lancashire's assessment approach, KLIPs, as summative judgements in relation to age related expectations. Definitions for these terms can be found in the introduction to the KLIPs document.

#### How might Learning and Progression Steps (LAPS) in Mathematics be useful?

Learning and Progression Steps (LAPS) may be used in a number of ways. For whole class teaching, LAPS may be used to support differentiation. When planning, it may be appropriate to use LAPS statements to inform learning objectives for a session or number of sessions. Learning and Progression Steps (LAPS) in Mathematics should be selected according to the learning needs of the individual or group. Emphasis however, should always be on developing breadth and depth of learning to ensure skills, knowledge and understanding are sufficiently embedded before moving on.

The LAPS should **not** be used as an assessment tool, but they can inform teachers about children's progress towards the end of year expectations at the end of each term.

## Are LAPS consistent with the other resources from the Lancashire Mathematics Team?

Yes, the LAPS are related to the content of the Mathematics Planning Support Disc and also the Progression Towards Written Calculation Policies and the Progression in Mental Calculation Strategies.

These can be found on the website:

www.lancsngfl.ac.uk/curriculum/primarymaths

# Key Learning in Mathematics – Year 4

Rey Learning in Mathematics Tear 4		
Number – number and place value	Number – addition and subtraction	Number – multiplication and division
<ul> <li>Count in multiples of 6, 7, 9, 25 and 1000</li> <li>Count backwards through zero to include negative numbers</li> <li>Count up and down in hundredths</li> <li>Read and write numbers to at least 10 000</li> <li>Read and write numbers with up to two decimal places</li> <li>Recognise the place value of each digit in a four-digit number</li> <li>Identify the value of each digit to two decimal places</li> <li>Partition numbers in different ways (e.g. 2.3 = 2+0.3 &amp; 1+1.3)</li> <li>Identify, represent and estimate numbers using different representations (including the number line)</li> <li>Order and compare numbers beyond 1000</li> <li>Order and compare numbers with the same number of decimal places up to two decimal places</li> <li>Find 0.1, 1, 10, 100 or 1000 more or less than a given number</li> <li>Round any number to the nearest 10, 100 or 1000</li> <li>Round decimals (one decimal place) to the nearest whole number</li> <li>Find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer</li> <li>Describe and avtand number same requestions involving counting on or back in</li> </ul>	<ul> <li>Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method)</li> <li>Select a mental strategy appropriate for the numbers involved in the calculation</li> <li>Recall and use addition and subtraction facts for 100</li> <li>Recall and use addition and subtraction facts for 1 and 10 (with decimal numbers to one decimal place)</li> <li>Add and subtract mentally combinations of two and three digit numbers and decimals to one decimal place</li> <li>Add and subtract numbers with up to 4 digits and decimals with one decimal place using the formal written methods of columnar addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why</li> <li>Solve addition and subtraction problems involving missing numbers</li> </ul>	<ul> <li>Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method)</li> <li>Recognise and use factor pairs and commutativity in mental calculations</li> <li>Recall multiplication and division facts for multiplication tables up to 12 × 12</li> <li>Use partitioning to double or halve any number, including decimals to one decimal place</li> <li>Use place value, known and derived facts to multiply and divide mentally, including: <ul> <li>multiplying by 0 and 1</li> <li>dividing by 1</li> <li>multiplying together three numbers</li> </ul> </li> <li>Multiply two-digit and three-digit numbers by a one-digit number using formal written layout</li> <li>Divide numbers up to 3 digits by a one-digit number using the formal written method of short division and interpret remainders</li> </ul>
<ul> <li>Describe and extend number sequences involving counting on or back in different steps, including sequences with multiplication and division steps</li> <li>Read Roman numerals to 100 and know that over time, the numeral system changed to include the concept of zero and place value</li> <li>Solve number and practical problems that involve all of the above and with increasingly large positive numbers</li> <li>Number – fractions and decimals</li> <li>Understand that a fraction is one whole number divided by another (e.g. <sup>3</sup>/<sub>4</sub> can be interpreted as 3 ÷ 4)</li> <li>Recognise, find and write fractions of a discrete set of objects including those with a range of numerators and denominators</li> <li>Recognise that hundredths arise when dividing an object by one hundred</li> </ul>	<ul> <li>Geometry – properties of shapes</li> <li>Compare and classify geometric shapes, including quadrilaterals and triangles, based on their properties and sizes</li> <li>Identify lines of symmetry in 2-D shapes presented in different orientations</li> <li>Complete a simple symmetric figure with respect to a specific line of symmetry</li> <li>Continue to identify horizontal and vertical lines and pairs of perpendicular and parallel lines</li> <li>Identify acute and obtuse angles and compare and order angles up to two right angles by size</li> </ul>	<ul> <li>appropriately for the context</li> <li>Use estimation and inverse to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy</li> <li>Solve problems involving multiplying and adding, including using the distributive law to multiply two digit numbers by one digit, division (including interpreting remainders), integer scaling problems and harder correspondence problems such as n objects are connected to m objects</li> <li>Measurement</li> <li>Estimate, compare and calculate different measures, including money in pounds and pence</li> </ul>
<ul> <li>and dividing tenths by ten</li> <li>Count on and back in steps of unit fractions</li> <li>Compare and order unit fractions and fractions with the same denominators (including on a number line)</li> <li>Recognise and show, using diagrams, families of common equivalent fractions</li> <li>Recognise and write decimal equivalents of any number of tenths or</li> </ul>	<ul> <li>Geometry – position and direction</li> <li>Describe positions on a 2-D grid as coordinates in the first quadrant</li> <li>Plot specified points and draw sides to complete a given polygon</li> <li>Describe movements between positions as translations of a given unit to the left/right and up/down</li> </ul>	<ul> <li>Order temperatures including those below 0°C</li> <li>Measure and calculate the perimeter of a rectilinear figure (including squares) in centimetres and metres</li> <li>Know area is a measure of surface within a given boundary</li> <li>Find the area of rectilinear shapes by counting squares</li> <li>Convert between different units of measure [e.g. kilometre to metre; hour to minute]</li> </ul>
Accognise and write decimal equivalents of any humber of tentrs o	<ul> <li>Statistics</li> <li>Use a variety of sorting diagrams to compare and classify numbers and geometric shapes based on their properties and sizes</li> <li>Interpret and present discrete and continuous data using appropriate graphical methods, including bar charts, time graphs</li> <li>Solve comparison, sum and difference problems using information presented in bar charts, pictograms, tables and other graphs</li> </ul>	<ul> <li>Read, write and convert time between analogue and digital 12-and 24-hour clocks</li> <li>Write amounts of money using decimal notation</li> <li>Recognise that one hundred 1p coins equal £1 and that each coin is 1/100 of £1</li> <li>Solve problems involving converting from hours to minutes; minutes to seconds; years to months; weeks to days and problems involving money and measures</li> </ul>

These Learning and Progression Statements (LAPS) are designed to show the necessary steps in learning to make effective and sustainable progress within a single year. They begin with the 'end of year' expectation from the previous year and build up to the 'end of year expectation' of the current year.

The number of steps is dependent on the learning and do **not** constitute expectations for the end of each term.

The steps are **not** of equal size and different amounts of time may be required for children to move between individual steps.

	End of Year 3 expectation				Lea	rning and Prog	ression Stateme	ents				End of Year 4 expectation
	Count from 0 in multiples of 4, 8, 50 and 100	Count in multiples of 1000 from 0 or any multiple of 1000		nt in multiple For any mult		Count in mult 0 or any m	iples of 9 from ultiple of 9				Count in multiples of 7 from 0 or any multiple of 7	Count in multiples of 6, 7, 9, 25 and 1000
	No equivalent objective in Year 3	La	abel positi	ive and nega	tive numbe	ers on a demarc	ated number lin	e (where t	he counting st	ep is one)	)	Count backwards through zero to include negative numbers
Number and Place Value	Count up and down in tenths	including where tenths (including where tenths boundaries are tencessed,	1) includ enths bour cross	undredths ing where ndaries are	redths fractional hundredt $\left(\frac{1}{100}\right)$ including where es are ones boundaries ar crossed,		(0.01) including whereequivaltenths boundaries arethecrossed,e.g. 1		equivalence the sequence e.g. 1.42, 2	Count up and down in Use knowledge of equivalence to refine the sequence, e.g. 1.42, 1.41, <u>1.4</u> , 1.39, 1.38 Count up and down in decimal hundredths (0.01) including where ones boundaries are crossed, e.g. 5.97, 5.98, 5.99, 6 6.01, 6.02		Count up and down in hundredths
	Read and write numbers up to 1000 in numerals and in words	Read multiples of 1000 to 10 000 in numerals and in words		Read multiples of 100 to 10 000 in numerals and in words Write multiples of 100 to 10 000 in numerals and in words		Read numbers to 10 000 where 0 is not used as a place holder Write numbers to 10 000 where 0 is not used as a place holder		holder 0 where 0 is	Read numbers to 10 000 where 0 is used as a place holder Write numbers to 10 000 where 0 is used as a place holder		Read <b>and write</b> numbers to at least 10 000	
Numb	Read and write numbers		place h	cimal places where 0 is not used as a ace holder			Read numbers with two decimal places where 0 is used as a place holder					Read and write numbers with up to
	with one decimal place	Write numbers with two	o decima place ł		re 0 is not ι	used as a	Write numbers with two decimal places where 0 is used as a place holder					two decimal places
	Recognise the place value of each digit in a three-digit number (hundreds, tens, ones)	Identify a four-digit number up to 10 000 made from concrete materials such as base 10 apparatus or representations of this					Make and identify a four-digit number up to 10 000 using models such as place value counters, an abacus and arrow cards					Recognise the place value of each digit in a four-digit number
	Identify the value of each digit to one decimal place	Use concrete materials to m number with two decimal p e.g. straws					Identify the value of each digit to two decimal places in a variety of ways e.g. the value of the digit 7 in 53.27 is seven hundredths, $\frac{7}{100}$ or 0.07Represent numbers to two decimal places using £1, 10p and 1p coins			Identify the value of each digit to two decimal places		

Partition numbers in different ways (e.g. 146 = 100+40+6 and 146 = 130+16)	represented using place value counters) into thousands, hundreds, tens and ones, e.g. 2643 is 2 thousands (2000), 6 hundreds, (600) 4 tens (40) and 3 ones (3) (represented using place value counters) hundreds, tens and ones, e.g. 2643 different thousand 1 hundred,			n a four-digit number ented using place value ers) into thousands, eds, tens and ones in nt ways, e.g. 2643 is 2 d 5 hundred (2500) and , 4 tens and 3 ones (143)	Anted using place value trs) into thousands, ds, tens and ones in t ways, e.g. 2643 is 2 5 hundred (2500) and 4 tens and 3 ones (143) Partition a four-digit nu without the use of pra- equipment into two gro different ways			actical different ways where one group is appropriate to the context e.g.	
130/10/	Partition numbers w (represented using s counters) into c e.g. 3.4 is 3 ones (3	straws or plac ones and tent	e value hs,	Partition numbers w (represented using s counters) into ones and e.g. 3.4 is 2 ones (2) and	Partition numbers with one decimal place without the use of practical equipment into two groups in different ways				
Identify, represent and estimate numbers using different representations	Identify and represent r to 10 000 using mode place value counters, an arrow cards	numbers up Is such as abacus and	Correctly p a numbe 1000 mark star	place multiples of 100 on In line with multiples of The but not labelled (with t and end labelled 0 and 10 000)	Correctly place any nu number line with multip marked but not labellec and end labelled 0 an	oles of 1000 d (with start	number lin marked b variety o	place any number on a e with multiples of 1000 ut not labelled (with a f start and end points g. 2500 to 7500)	Identify, represent and estimate numbers using different
(including the number line)	Identify and represent numbers with up to two decimal places using models such as straws, place value counters and arrow cards			Correctly place multiple number line with mult not labelled (wi labelled	Correctly place multiples of one hundredth (0.01) on a number line with multiples of 0.1 marked but not labelled (with start and end labelled 0 and 1)			representations (including the number line)	
Compare and order numbers up to 1000	Compare two number 10 000 when represen models such as plac counters saying which greater or less and use correctly. Pay particula to numbers that have digits, e.g. 2634 and	e value number is <, > and = r attention the same	up to 10 using mod counters sa greater of correctly. to number	three or more numbers 000 when represented dels such as place value aying which numbers are r less and use <, > and = Pay particular attention rs that have some of the same digits, 3615 < 3652 > 3625	Order numbers up to 1 different numbers of d represented using mod place value counters sa numbers are greate	igits, when lels such as lying which	different n	nbers up to 10 000 with umbers of digits, saying abers are greater or less	Order and compare numbers beyond 1000
Compare and order numbers with one decimal place	Compare two or more numbers with tenths and hundredths using concrete materials such as straws, saying which has more and less and use <, > and = correctly. Pay particular attention to numbers that have the same digits, e.g. 0.23 and 0.32	using co material straws, saa numbers a or l Pay pa attention t that ha same	nbers with hundredths oncrete s such as ying which	Compare two or more numbers with ones, tenths and hundredths using concrete materials such as straws, saying which has more and less and use <, > and = correctly. Pay particular attention to numbers that have the same digits, e.g. 1.56, 1.65 and 6.15	Order numbers with ones, tenths and hundredths using concrete materials such as straws, saying which numbers are greater or less. Pay particular attention to numbers that have the same digits, e.g. 5.61, 1.56 and 6.15	with the sa of decin saying wh is more or <, > and = Pay pa attention that have digits, e.g.	e numbers me number nal places ich number less and use correctly. inticular to numbers e the same 115.62 and 1.52	Order numbers with the same number of decimal places saying which numbers are greater or less. Pay particular attention to numbers that have the same digits, e.g. 65.12, 21.56 and 26.15	<i>Order and</i> compare numbers with the same number of decimal places up to two decimal places
Find 1, 10 or 100 more or less than a given number	Identify the number 10 given number with up t which digits sta which dig	o four-digits	recognising	Identify the number or less than a given numbe place, where the ones	he tenth (0.1) more and er with up to one decimal digit stays the same e.g. nore than 2.4	Identify the number one tenth (0.1) more and less than a given number with up to one decimal place, where the ones digit changes e.g. one tenth less than 6		Find <i>0.1, 1, 10, 100 or</i> 1000 more or less than a given number	

	Round numbers to at ist 1000 to the nearest 10 or 100	Identify the multiple of 10 immediately before and after a given four-digit number	, Round nun	digits to the n, e.g. 4356	of 10 befo give	fy the multiples 0 immediately re and after a en four-digit number	up to fou nearest h	umbers with r-digits to the nundred, e.g. unds to 4400	e of 1000 befor give	the multiples ) immediately e and after a n four-digit number	Round numbers with up to four-digits to the nearest thousand, e.g. 4356 rounds to 4000	Round any number to the nearest 10, 100 or 1000
	Round numbers to at 1st 1000 to the nearest 10 or 100	Identify the whole n and after a number the numb		lace where	Round	d numbers with o nearest whole the number i	number wh	iere		dentify the whole numbers immediately before and after a number to one decimal place where		Round decimals (one decimal place) to the nearest whole number
tv	Find the effect of nultiplying a one- or vo-digit number by 10 and 100, identify the lue of the digits in the answer	Use concrete materials to model the effect of dividing a one- digit number by 10 e.g. exchange each straw for a tenth of a straw and identify what changes	Describe the effect of dividing a one- digit number by 10, e.g. 7 ÷ 10 = 0.7 The 7 has moved one place to the right; from the ones column to the tenths column. A place holder (zero) is needed in the ones column	Use concr materials model th effect of dividing a to digit numb 10 e.g exchange of bundle of straws for single stra and each s for a tenth straw ar identify w changes a what sta the sam	s to he of two- er by each tran aw, of a aw, of a hd traw hat and ys	Describe the effect of dividing a two- digit number by 10, e.g. 73 ÷ 10 = 7.3 Both digits have moved one place to the right	Use con materia model effect dividing a digit num 100 e exchange straw f hundred straw identify changes what s the sa	crete als to d the di the di to one- 7 ber by e.g. e each p to r a ri th of a or and th what co s and he tays n	Describe the effect of ividing a one git number b 100, e.g. ÷ 100 = 0.07 The 7 has moved two places to the ght; from the hes column t is hundredth dumn. A plac plder (zero) i seeded in the hes and tenth columns	materials i model the effect of dividing a tw digit numbe 100 e.g. exchange ea bundle of t straws for tenth straw, each straw for s hundredth o straw and s digit numbe	vo- by by by child by child by child by child by child by child by child by child ch	Find the effect of dividing a one- or two- digit number by 10 and 100, identifying the value of the digits in the answer
in	Describe and extend number sequences volving counting on or ack in different steps		plete sequences, i re addition / subt ) or multiplication	raction	/ divis	y and describe the sion number sequ ionship between t	ence by ide	entifying the		· · · · · · · · · · · · · · · · · · ·		Describe and extend number sequences involving counting on or back in different steps, including sequences with multiplication and division steps
R	ead Roman numerals from I to XII	Know that L represents 50 and C represents 100	Represent numbers with o additive proper i.e. not ending or 9	only befo ties repr in 4 thar	w that I c nly be use re V and 1 resent 1 l n 5 (4) an s than 10	ed X to Repress ess number d 1		Know tha only be before L a represent than 50 (4 10 less 100 (1	used and C to 10 less 40) and than	Represent any number up to 100	Compare and contrast Roman numeral system and modern day number system	Read Roman numerals to 100 and know that over time, the numeral system changed to include the concept of zero and place value
aı	lve number problems nd concrete problems nvolving these ideas	See	Children need frequent access to arrange of contexts using the content from all of the above. ee Using and Applying, Contextual Learning and Assessment section form the Lancashire Mathematics Planning Disc.					Solve number and practical problems that involve all of the above and with increasingly large positive numbers				

	End of Year 3 expectation			Learning and F	Progression Statements			End of Year 4 expectation			
	Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method)		Children need frequent opportunities to select appropriate strategies from the range they have learnt. The most efficient strategy may differ between children as it will be based on their confidence and competence. These steps fit the Lancashire Progression Towards Written Calculation Policies and Progression in Mental Calculations Policies								
Number – Addition and Subtraction	Select a mental strategy appropriate for the numbers involved in the calculation	method)These steps fit the Lancashire ProgressionThese steps fit the Lancashire ProgressionSelect a mental trategy appropriate for the numbers involved in the calculationRecognise and solve calculations that involve known or related facts e.g. 250 + 130Recognise that the numbers in calculations can be efficient e.g. 18 + 6 - 8 becomes 18 - 8 + 6 to and use this strategy where appropriate (This should be supported by concrete materials, contract		Recognise calculations that require counting on or back mentally e.g. 243 + 230 (counting on in hundreds and then in tens) and use this strategy where appropriate (This should be supported by concrete materials, pictures or jottings)	Recognise calculation Policies and require mental partitioning e.g. 122 - 35 and use this strategy where appropriate (This should be supported by concrete materials, pictures or jottings)	Recognise calculations that require counting on mentally to find the difference e.g. 203 – 96 and use this strategy where appropriate (This should be supported by concrete materials, pictures or jottings)	Recognise calculations that require counting on or back mentally, bridging through a multiple of 10 efficiently e.g. $230 - 72$ becomes 230 - 30 - 40 - 2 and use this strategy where appropriate ( <i>This should be supported by</i> <i>concrete materials, pictures</i> <i>or jottings</i> ) Recognise calculations that require a mental compensation method e.g. $213 - 58$ becomes 213 - 60 + 2 and use this strategy where appropriate ( <i>This should be supported by</i> <i>concrete materials, pictures</i> <i>or jottings</i> )	Select a mental strategy appropriate for the numbers involved in the calculation			
	Derive and use addition and subtraction facts for 100			There are no steps towa	ards this end of year expe	ectation		Recall and use addition and subtraction facts for 100			
	Derive and use addition and subtraction facts for multiples of 100 totalling 1000			There are no steps towa	ards this end of year expe	ectation		Recall and use +/- facts for multiples of 100 totalling 1000			
	Derive and use addition and subtraction facts for 100 Derive and use addition and subtraction facts for multiples of 100 totalling 1000		n and subtraction facts for ar model and related facts	10 using nur	tion and subtraction facts nber lines, bar model related facts	Recognise that,	when calculating addition facts s total 9 and the tenths total 1	Derive and use addition and subtraction facts for 1 and 10 (with decimal numbers to one decimal place)			

Add and subtract numbers mentally, including: - a three-digit number and ones - a three-digit number and tens - a three-digit number and hundreds	Add and subtract a two-digit number to/from another two-di number including crossing the hundreds boundary, e.g. 87 + 35 (This could be supported by jottin or a number line) Add and subtract a number wit place to/from a whole numbe (This could be supported b or a number line,	Add and subtract a three-digit number to/from a three-digit number to/from a three-digit number where no boundaries are crossed, e.g. 765 – 241 (This could be supported by jottings r line)Add and subtract a two-digit number to/from a three-digit number vhere no boundaries are crossed, e.g. 765 – 241 (This could be supported by jottings or a number line)Add and subtract a two-digit number to/from a three-digit number including crossing th hundreds boundary, e.g. 122 – (This could be supported by jottings or a number line)Add and subtract a two-digit number including crossing th hundreds boundary, e.g. 122 – (This could be supported by jottings or a number line)number with one decimal hole number, e.g. 6.3 + 4 supported by jottingsAdd and subtract a number where the ones boundary is not crossed, e.g. 5.8 – 2.5 (This could be supported by iottings)Add			ree-digit ssing the g. 122 – 35 by jottings e) Add and s place to/fro	nu nur hundi (This of om anot is cross could b	d and subtract a three-digit mber to/from a three-digit mber including crossing the reds boundary, e.g. 205 – 197 could be supported by jottings or a number line) a number with one decimal her where the ones boundary ed, e.g. 14.7 + 8.6 e supported by jottings a number line)	Add and subtract mentally combinations of two and three digit numbers and decimals to one decimal place		
Add and subtract numbers with up to three digits, using formal written	Add two numbers with four digits using formal written methods of columnar addition with exchange e.g. 2326 + 3845	Add more thar numbers with fou using formal w methods of colu addition with exc e.g. 2468 + 3326	ur digits ritten umnar change, + 3782	Add more numbers wit digits using fo method of addi e.g. 673 + 5	than two th up to four ormal written columnar tion,	decimal writt colu wi	numbers wit place using for ten methods imnar additio th exchange, g. 54.7 + 73.6	h one ormal of n	Add more than two numbers with up to one decimal place using formal written methods of columnar addition with exchange, e.g. 268 + 34.7 + 356.5	Add and subtract numbers with up to 4 digits and decimals with one decimal place using the formal
methods of columnar addition and subtraction	Subtract two numbers with fou digits using formal written metho of columnar subtraction with exchange e.g. 3845 - 2588	ts using formal written methods of columnar subtraction with			Subtract two numbers with one decimal place using formal written methods of columnar subtraction with exchange, e.g. 63.7 - 37.8			tract two numbers with one nal place using formal written ods of columnar subtraction exchange where the greater ober has 0 as a place holder, e.g. 50.7 - 23.8	written methods of columnar addition and subtraction where appropriate	
Estimate the answer to a calculation and use inverse operations to check answers	Use rounding to estimate the ans be estimated	wer to a calculati as 2400 + 400 = 1	-	23 + 389 could		be checke		out eith s correc		Estimate; use inverse operations to check answers to a calculation
Solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction		•	en need frequent access to arrange of contexts using the content from all of the above. lying, Contextual Learning and Assessment section form the Lancashire Mathematics Planning Disc.						Solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why	
Solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction	Rep	Represent and solve a problem using structured pictorial representations such as the bar model								Solve addition and subtraction problems involving missing numbers

	End of Year 3 expectation				Lea	Irning and Prog	ression State	ments					End of Year 4 expectation
	Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method)					inities to select appropriate strategies from the range they have learnt. er between children as it will be based on their confidence and competence							Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method)
-	Understand how multiplication and division statements can be represented using arrays					to identify all the factor of a given number within the multiplication tables that they know					Recognise and use factor pairs and commutativity in mental calculations		
	Recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables	Recall and use multip and division facts for multiplication tal	r the 6 and	Recall and use multiplic and division facts for th multiplication table		r the 11 and division fac		facts for the 9 and divi		d use multiplication sion facts for the 7 iplication table multiplication table		Recall multiplication and division facts for multiplication tables up to 12 × 12	
	Derive and use doubles of all numbers to 100 and corresponding halves Derive and use doubles of all multiples of 50 to 500	Use partitioning to double any number with up to four digits where the answer is less than 10 000	Use related fa double a nu of tenth e.g. double	nber do	haive an umber with ones and tenths, e.g. double 6.8 haive an number digit haive an number digit Recognise the between a kr related ca		Use partitioning to halve any four digit bumber where each digit is even under where each dig		ur digit r where digits . 4524 itioned 20 + 4 use partitioning to halve a number with ones and tenths where both digits are even		Use partitioning to halve any number with ones and tenths where the tenths digit is even e.g. half of 3.6 could be partitioned into 3 + 0.6 or 2 + 1.6	Use partitioning to double or halve any number, including decimals to one decimal place	
-		Recognise that multi by 0 gives a produc	piying	umber by 1 d			e relationship own fact and culation e.g. 600 x 4 = 240	Represe three n e.g. 2 x	4400 + 100 + 24 Represent multiplication of three numbers using arrays e.g. 2 x 3 x 4 can be shown using a 2 x 3 array four times		three numbers to simplify the calculation e.g.		Use place value, known and derived facts to multiply and divide mentally, including:
		Recognise that dividing a number by 1 does not change the number       Use knowledge of place value and multiplication facts to divide related greater numbers e.g. 630 ÷ 9 = 70       Divide a two-digit number by a one-digit number using a partitioning strategy e.g. 96 ÷ 4 becomes (80 ÷ 4) + (16 ÷ 4)					- multiplying by 0 and 1 - dividing by 1 - multiplying together three numbers						

k	Vrite and calculate mathematical statements for multiplication and division using the multiplication tables that they mow, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods	Use	Use partitioning to calculate a three-digit number multiplied by a single digit number using grid method								
k	Vrite and calculate mathematical statements for multiplication and division using the multiplication tables that they mow, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods	Divide two-digit numbers (beyond the multiplication facts) by a single digit number using the chunking method where there is no remainder e.g. 72 ÷ 4	Divide two-digit numbers (beyond the multiplication facts) by a single digit number using the chunking method where there is a remainder e.g. 56 ÷ 3	Divide three- by a single c using the chur where there is e.g. 24	ligit number nking method	Divide three-digit numbers by a single digit number using the chunking method, making the calculation more efficient by subtracting more than one multiple of 10 of the divisor e.g. 248 ÷ 4 by subtracting 240 (60 groups of 4) and 8 (2 groups of 4)	Divide three-digit numbers by a single digit number efficiently using the chunking method where there is a remainder e.g. 176 ÷ 6	Divide numbers up to 3 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context			
	Use estimation to check answers to calculations and determine, in the		inding to the nearest multiple of d facts e.g. 384 x 6 ≈ 400 x 6	10 or 100 and	to check the answer to a calculati ked by carrying out the following ÷ 6 (performed using a calculator	calculation correctly:	Use estimation and inverse to check answers to calculations				
a	context of a problem, an ppropriate degree of accuracy		to the nearest multiple of 10 of t d facts e.g. 352 ÷ 6 ≈ 360 ÷ 6	the divisor and	Use inverse chec	and determine, in the context of a problem, an appropriate degree of accuracy					

Solve problems,			
including missing		Solve problems	
number problems,		involving multiplying	
involving		and adding, including	
multiplication and		using the distributive	
division (and		law to multiply two	
interpreting		digit numbers by one	
remainders),	Children need frequent access to arrange of contexts using the content from all of the above.	digit, division	
including positive	See Using and Applying, Contextual Learning and Assessment section form the Lancashire Mathematics Planning Disc.	(including interpreting	
integer scaling		<i>remainders),</i> integer	
problems and		scaling problems and	
correspondence		harder correspondence	
problems in which		problems such as n	
n objects are		objects are connected	
connected to m		to m objects	
objects			

	End of Year 3 expectation			Learning and P	ogression Stateme	ents			End of Year 4 expectation				
	Show concretely or pictorially that a fraction is one whole number divided by another (e.g. $\frac{3}{4}$ can be interpreted as $3 \div 4$ )	This	This is consolidation of Year 3 learning and therefore there are no steps towards this end of year expectation										
suo	Recognise, find and write fractions of a discrete set of objects: unit fractions and non- unit fractions with small denominators	tions of a e set of s: unit and non- ions withWhere a fraction of an amount cannot be found by using known division facts, use pictorial representations, e.g. bar model, to find non-unit fractions and non- ions withFind non-unit fractions of an amount cannot be found by using known division fracts, use pictorial representations, e.g. bar model, to find non-unit fractions and non- ions withFind non-unit fractions of an amount cannot be found by using known division fracts, use pictorial representations, e.g. bar model, to find non-unit fractions and non- ions withFind non-unit fractions of an amount cannot be found by using known division fraction then multiplying to scale up by the numerator e.g. $\frac{4}{7}$ of 315 by calculating 315 ÷ 7 to find $\frac{1}{7}$ of 315 which is 45 then 45 x 4 to find $\frac{4}{7}$ of 315 which is 180								facts, use pictorial representations, e.g. bar model, to find non-unit fractions			Recognise, find and write fractions of a discrete set of objects including those with a range of numerators and denominators
Number – Fractions	Recognise that tenths arise from dividing objects into 10 equal parts and in dividing one- digit numbers or quantities by 10	from ects parts g one- rs orUse pictorial representations such as a 10 x 10 grid to show that $\frac{1}{100}$ of an object can be found by dividing the object into one hundred equal partsUse pictorial representations such as a 10 x 10 grid to recognise that $\frac{1}{100}$ of an object can be found by dividing $\frac{1}{10}$ of the object into ten equal parts							Recognise that hundredths arise when dividing an object by one hundred and dividing tenths by ten				
	Count on and back in steps of $\frac{1}{2}$ , $\frac{1}{4}$ and $\frac{1}{3}$	boundaries e.g. on			of any unit fraction bundaries e.g. $\frac{1}{9}$ , $1, \frac{7}{9}, \frac{6}{9}, \frac{5}{9}$	crossing	fractions in th	quivalence to begin to simplify e counting sequence e.g. , 1, $1\frac{1}{8}$ , $1\frac{1}{4}$ , $1\frac{3}{8}$ , $1\frac{1}{2}$	Count on and back in steps of unit fractions				
	Compare and order unit fractions, and fractions with the same denominators (including on a number line)			r 3 learning and theref	bre there are no ste	ps towards t			Compare and order unit fractions and fractions with the same denominators (including on a number line)				
	Recognise and show, using diagrams, equivalent fractions with small denominators	fractions are equivale	Use pictorial representations such as fraction walls to recognise where fractions are equivalent where one fraction is a unit fraction e.g. $\frac{1}{6}$ is the same as $\frac{3}{18}$ Use pictorial representations such as fraction walls to recognise where fractions are equivalent where both fractions are non-unit fractions e.g. $\frac{3}{4}$ is the same as $\frac{9}{12}$										
	No equivalent objective in Year 3	Understand the hundredths heading in place value columns represents a given number of fractional hundredths, e.g. $\frac{3}{100}$ is equal to 0.03	Recognise and write equivalents for any of hundredths less e.g. $\frac{7}{100}$ is 0.0	number Recogn than 10/100 equival	ise that $\frac{10}{100}$ is ent to $\frac{1}{10}$ or 0.1	equiva	gnise that $\frac{20}{100}$ is alent to $\frac{2}{10}$ or 0.2 and so on	Write any number of hundredths in fraction and decimal form e.g. $rac{47}{100}$ is 0.47	Recognise and write decimal equivalents of any number of tenths or hundredths				

Recognise and show, using diagrams, equivalent fractions with small denominators	Use concrete materials (such as money) or pictorial representations (such as a 10 x 10 grid) to show that $\frac{1}{2}$ is the same as $\frac{50}{100}$ which is 0.50 or 0.5		als (such as money) or (such as a 10 x 10 grid) to the as $\frac{25}{100}$ which is 0.25	Use concrete materials (such as money) or pictorial representations (such as a 10 x 10 grid) to show that $\frac{3}{4}$ is the same as $\frac{75}{100}$ which is 0.75	Recognise and write decimal equivalents to $\frac{1}{4}$ , $\frac{1}{2}$ , $\frac{3}{4}$				
Add and subtract fractions with the same denominator within one whole [for example, $\frac{5}{7} + \frac{1}{7} = \frac{6}{7}$ ]	Use pictorial representations, such as fraction str fractions with the same denominator crossin e.g. $\frac{5}{7} + \frac{4}{7} = \frac{9}{7}$	· • · · · ·	Add and subtract fra boundary by addi	Add and subtract fractions with the same denominator ( <i>using</i> <i>diagrams</i> )					
Solve problems that involve all of the above			cess to arrange of contexts using the content from all of the above. Parning and Assessment section form the Lancashire Mathematics Planning Disc cess to arrange of contexts using the content from all of the above. Parning and Assessment section form the Lancashire Mathematics Planning Disc						
No equivalent objective in Year 3									

	End of Year 3 expectation	Learning and Progression Statements								
Geometry – Properties of Shapes	Draw 2-D shapes and make 3-D shapes using modelling materials; recognise 3-D shapes in different orientations and describe them	vertices – number of vertices scalene, is scalene, is				ame 2-D shapes including all triangles and adrilaterals according to their properties		Compare and classify geometric shapes, including quadrilaterals and triangles, based on their properties and sizes		
		Identify properties of 3-D shapes including: faces or surfaces – number of faces and/or surfaces, where any are congruent (identical), parallel and perpendicular edges – number of edges, parallel and perpendicular vertices – number of vertices axis of symmetry		Name 3	Name 3-D shapes including all prisms and pyramids according to their properties					
	No equivalent objective in Year 3	Identify a vertical or horizontal line of symmetry in a shape			From a set o	From a set of shapes, identify those with a vertical or horizontal line of symmetry and those without			Identify lines of symmetry in 2-D shapes presented in different orientations	
	No equivalent objective in Year 3	Complete a simple symmetric figure using a vertical or horizontal line of symmetry				Complete a simple symmetric figure where the line of symmetry is not vertical or horizontal will dissect the figure			Complete a simple symmetric figure with respect to a specific line of symmetry	
	Identify horizontal and vertical lines and pairs of perpendicular and parallel lines	This is co		there are no steps towards this end of year expectation			Continue to identify horizontal and vertical lines and pairs of perpendicular and parallel lines			
	Identify right angles, recognise that two right angles make a			nd obtuse angles lines is horizontal		nd obtuse angles e lines is vertical		d obtuse angles in entation		
	half-turn, three make three quarters of a turn and four a complete turn; identify whether angles are greater than or less than a right angle	Know that an angle less than a right angle is called 'acute' Know that an angle between a right angle and a straight angle is called 'obtuse'	Compare any two angles less than two right angles where one of the lines is horizontal, identifying which is greater and less	Order more than two angles less than two right angles where one of the lines is horizontal	Compare any two angles less than two right angles where one of the lines is vertical, identifying which is greater and less	Order more than two angles less than two right angles where one of the lines is vertical	Compare any two angles less than two right angles in any orientation, identifying which is greater and less	Order more than two angles less than two right angles in any orientation	Identify acute and obtuse angles and compare and order angles up to two right angles by size	

	End of Year 3 expectation		End of Year 4 expectation			
	Describe positions on a square grid labelled with letters and numbers	Know that the x axis is horizontal	Know that vertical lines on a grid can be identified by the value on the x axis from which they originate		Know that the first number in a coordinate pair refers to the x value and the second number	Describe positions on a 2-D grid as coordinates in the first quadrant
rection		Know that the y axis is vertical	Know that horizontal lines on a grid can be identified by the value on the y axis from which they originate		refers to the y value and read and write them using correct notation e.g. ( x , y )	
Geometry – Position and Dir	Describe positions on a square grid labelled with letters and numbers	Plot a single point on a coordinate grid from a	given coordinate pair	Plot	Plot specified points and draw sides to complete a given polygon	
	No equivalent objective in Year 3	Describe movement of a spe	Describe movements between positions as translations of a given			
		Describe movement of a sp	pecified point as a translatio	n of a given unit using up a	nd down e.g. six squares up	unit to the left/right and up/down

	End of Year 3 expectation	Learning and Progression Statements						
Statistics	Use sorting diagrams to	Use Venn diagrams with two intersecting sets to compare and sort objects, numbers and shapes including items that do not fit the criteria and placing these in the universal set (area outside the circles)						Use a variety of sorting diagrams to compare and classify numbers and geometric shapes based on their properties and sizes
	compare and sort objects, numbers	Use two criteria Carroll diagrams to compare and sort objects, numbers and shapes (understanding that Carroll diagrams are labelled 'is' and 'is not')						
	and common 2-D and 3-D shapes	NB – the criteria used for comparing and sorting should be consistent with the properties from the Year 4 curriculum e.g. multiples of 7 and even number or regular and contains at least one acute angle						
	Interpret and present data using bar charts, pictograms and tables	Interpret and present discrete data using bar charts and a scale appropriate to Year 4 counting and place value	Choose the appropriate scale when representing data in a bar chart	Explain what a time graph is showing e.g. a child might describe temperature increasing or decreasing at different times during a day		Present time graphs from given data using appropriate scales	Understand that discrete data that can only take specific, separate values and the data sets are not related to each other Understand that continuous data is data that can take on any value along a continuum	Interpret and present discrete and continuous data using appropriate graphical methods, including bar charts, time graphs
	Solve one-step and two-step questions [for example, 'How many more?' and 'How many fewer?'] using information presented in scaled bar charts and pictograms and tables	Answer questions using time graphs by reading from labelled values e.g. what was the temperature at 3:00pm (where each hour is labelled on the x axis)				ons using time graphs by readin s the temperature at 1:30pm (w the x axis)	g from between labelled values here each hour is labelled on	Solve comparison, sum and difference problems using information presented in bar charts, pictograms, tables and other graphs

End of Year 3 expectation	Learning and Progression Statements					End of Year 4 expectation			
	Measure lengths (m/cm/mm) use known measurements to n reasonable estimates includi numbers to two decimal plac	nake objects including nur	mbers to two	the differen including nu place (see progre	ract (including finding nce) values of length mbers to one decimal e (m/cm/mm) ession in mental and dition / subtraction)	(se	ply and divide values of length (m/cm/mm) e progression in mental and ten multiplication / division)	Estimate, compare and calculate different measures, including money in pounds	
Measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g);	Measure mass (kg/g) and use kr measurements to make reason estimates including numbers to decimal places	able Compare the mass	mbers to two	the differe including nu p (see progre	ract (including finding nce) values of mass mbers to one decimal lace (kg/g) ession in mental and dition / subtraction)	(se	iply and divide values of mass (kg/g) e progression in mental and ten multiplication / division)		
volume/capacity (I/mI)	Measure volume/capacity (I/ml use known measurements to n reasonable estimates includi numbers to two decimal plac	nake different objects inclu	iding numbers	the diffe volume/capa to one de (see progre	Add and subtract (including finding the difference) values of volume/capacity including numbers to one decimal place (I/mI) (see progression in mental and written addition / subtraction)		ultiply and divide values of volume/capacity (I/mI) e progression in mental and ten multiplication / division)	and pence	
	Add and subtract amounts of money including money notation where the pence is a multiple of 10p e.g. £24.60 + £8.50 (see progression in mental and written addition / subtraction)Multiply and divide amounts of money given in pence only e.g. 45p x 4 (see progression in mental and written addition / subtraction)								
Continue to estimate and measure temperature to the nearest degree (°C) using thermometers	Place temperatures including negative numbers on a number line (this could be vertical)					Order temperatures including those below 0°C			
Understand perimeter is a measure of distance around the boundary of a shape Measure the perimeter of simple 2-D shapes	Recognise where sides are the same length in a rectangles, including squares and use this when measuring and calculating perimeter e.g. perimeter of a square is length of one side multiplied by 4; the perimeter of an oblong is the length + the width multiplied by 2			Recognise where the sides are the same length in L and T shaped rectilinear figures and use this when measuring and calculating perimeter Calculate the length of missing sides using known dimensions (see progression in mental and written addition / subtraction)		Measure and calculate the perimeter of a rectilinear figure (including squares) in centimetres and metres			
No equivalent objective in Year 3	There are no steps towards			this end of year expectation			Know area is a measure of surface within a given boundary		
No equivalent objective in Year 3	snapes (including those with where the sides are find the area		ge of arrays to of rectangles by ares in groups Find the area of other rectilinear shapes presented on squared paper where the sides are horizontal and vertical by counting squares in groups		Find the area of rectilinear shapes by counting squares				

Measurement

No equivalent objective in Year 3	Know that: 10mm = 1cm 100cm = 1m 1000m = 1km and vice versa Know that: 1000g = 1kg and vice versa Know that: 1000ml = 1 litre and vice versa Know that: 60 seconds = 1 minute 60 minutes = 1 hour 24 hours = 1 day 7 days = 1 week		Use the relationship between diffical calculation necessary for conversion divide the number NB – there is no requirement in Yer Therefore when converting from mt related facts and whole numbers of NB – there is no requirement in Yer Therefore when converting from gt related facts and whole numbers of NB – there is no requirement in Yer Therefore when converting from mt related facts and whole numbers of Use the relationship between diffical calculation necessary for conversion minutes, multiply the NB – when multiplying by 24 or 60, to e.g. how many	Convert between different units of measure [e.g. kilometre to metre; hour to minute]	
Tell and write the time from an analogue clock, including using Roman numerals from I to XII, and 12-hour and 24- hour clocks	Know that 24 hour clock times are written using four digits e.g. 8:35am is 08:35 or 0835	written using four digits e.g. 8:35am between 0 and 12 are before midday (morning) and times between 12 and		r to smaller units using multiplication Tell the time on a 24-hour clock, e.g. 16:27 is 27 minutes past 4 in the afternoon	Read, write and convert time between analogue and digital 12- and 24-hour clocks
Continue to recognise and use the symbols for pounds (£) and pence (p) and understand that the decimal point separates pounds/pence		relate to money notation i.e. units/ones co quivalent 10p coins; hundredths column re		Write amounts of money using decimal notation	
Recognise that ten 10p coins equal £1 and that each coin is $\frac{1}{10}$ of £1	Recognise that one hu	ndred 1p coins equal £1	Recognise that each 1p coin is $\frac{1}{100}$ of which is consistent with the o	Recognise that one hundred 1p coins equal £1 and that each coin is $\frac{1}{100}$ of £1	

Solve problems		
involving money		Calue muchlame
and measures and		Solve problems
simple problems		involving converting
involving passage		from hours to minutes;
	Children need frequent access to arrange of contexts using the content from all of the above.	minutes to seconds;
of time	See Using and Applying, Contextual Learning and Assessment section form the Lancashire Mathematics Planning Disc.	years to months;
Add and subtract		weeks to days and
amounts of money		problems involving
to give change,		
using both £ and p		money and measures
in practical contexts		
	1	